



# **Active Optics–Freeform Segment Mirror Replications from** a Deformable Matrix <sup>+</sup>

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Abstract: We present a new active optics method for making smooth aspheric, or freeform, mirrors by replication technique from an elastically deformable matrix. The mirror replicas provide an equivalent aberration correction to that of an off-axis segment of a Schmidt plate. The method describes geometry of a chromium stainless steel deformable matrix. Polished flat at rest, the matrix was used as submaster when in a bent state for single replications on a glass substrate. Two plane-aspheric segment mirror replicas are then used as a pair of correctors for a spectrograph telemeter. Located outside the Schmidt plate, in opposite diametric directions, the mirror replicas allow aberration compensation of the singlet convex-plane lens used both as collimator and cameraoptics of a spectrograph where the beams are passed twice. The spectrograph design is a "white pupil mounting" for a Cassegrainian telescope. The detector focusing is controlled by fusion imaging from the two mirror replicas. Our results show that the He-Ne beams wave-front error performed by the spectrograph, with each of the two replica mirrors passed twice, compensates at least 93% of the required total aspheric sag. This provides satisfactory results for the telemeter focusing device, which then is quasi-diffraction-limited. A similar replication technique is proposed to obtain a pair of off-axis Schmidt plates for a unit magnification Schmidt-Offner "ideal imager". Such a system is well suited for Laser Guide Star adaptive optics applications in modern astronomy.

**Keywords:** freeform mirror; aspheric; active optics; elasticity theory; optical design; mechanical design; replication techniques

# 1. Introduction

We hereby describe *freeform Schmidt mirrors* designed and built by a new active optics method for the telemeter segment-mirrors of the CFHT CassHawEC spectrograph that we had no time to present before because of a lack of time. It was the time when Baranne designed this spectrograph around 1980 for a Lallemand-Duchesne electronic camera (EC), thus, just before CCD camera advent.

The main reason for this paper comes from Rakich [1,2] discovering "ideal imaging" transport systems, called Schmidt-Reed-Offner or briefly Schmidt-Offner relays, where off-axis portions of a Schmidt plate allow correcting at least all third-order aberrations, i.e., Seidel aberrations. These telecentric unit-magnification imagers provide as well finite object conjugates as finite pupil conjugates. Theses *absolute instrument* properties are achieved by using an additional *freeform Schmidt plate*. Rakich previously investigated optical design cases of many reflecting anastigmatic optical systems and published a retrospective study of such systems [3].

Compared to the classical case of a Schmidt system using an aspheric corrector as first element, research on the best angular resolution for the case of all-reflective—or including a reflective grating—off-axis Schmidt systems led to the discovery of a new location of



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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). the null-power zone for the field aberration optimization. This elliptic zone must be  $\sqrt{3/2} = 1.224$  times larger than that of the clear aperture. The results by Lemaitre [4] were applied to the design of wide-field spectrographs and to the design and construction of the giant 4-m reflective Schmidt telescope LAMOST by Wang, Su et al. [5] for fiber-fed spectroscopic surveys in Xinlong Observatory.

Lemaitre showed also in "Astronomical optics and elasticity theory-Active optics methods" [6] that large manifolds of optical shapes can be generated. These methods apply to lenses, mirrors, and diffraction gratings by using either stress polishing at lab, or in situ stressing, or replication techniques with deformable matrices. Active optics methods based on elasticity theory of thin plates were investigated by Lemaitre leading to new solutions for generating toroid surfaces with *vase forms* [7]. A more recent proposal was investigated for ultraviolet instruments FIREBall and MESSIER [8]. Expected to be launched in 2022, FIREBall is a 1 m telescope with multi-object spectrograph whose goal is to detect Ly-alpha emission lines around galaxies; the disperser is an elliptical symmetry freeform reflective grating is deposited on the unstressed matrix. MESSIER proposal is a three-mirror all-reflective Schmidt telescope whose goal is to provide a clean spread-function imaging by avoiding any diffractive element through the beams; its optical design is optimized for curve detectors. The freeform correcting mirror is a hollow double vase-form with elliptical symmetry, which allows aspherization by stress polishing.

The present method was designed, a long time ago, for making smooth freeform optical surfaces either for obtaining reflective or refractive replicas. This is an answer to the question posed by Rakich for the complete design of its "ideal imager" with freeform corrector plates for Laser Guide Star Adaptive Optics (LGSAO) applications in modern astronomical observatories [1,2].

### 2. Generating a Telemeter Mirror Pair for CFHT CassHawEC Spectrograph

An active optics method was developed years ago (around 1982) for making freeform mirror segments that, due to lack of time, we did not present earlier. This method provided an equivalent aberration correction to that of the spectrograph Schmidt plate but located off-axis the plate clear aperture. The spectrograph design is a Baranne's *white pupil mounting* [9] that uses a cross-disperser made of a Carpenter-prism transparent grating and an echelle reflective grating. It receives the optical beam of a Cassegrain telescope focus at f/8 and was installed at CFHT in 1984.

The white pupil mounting was invented by Baranne [10], in French *montage à pupille blanche*, and provides the optical conjugation imaging of the pupils. The input pupil of the telescope primary mirror is reimaged at the diffractive element, and can be potentially reimaged by a successive image transport system from the previous dispersive element to the next dispersive cross element pupil. In most cases, the accurate pupil conjugation is achieved by a field lens. White pupil mounting spectrographs are widely adopted in astronomy.

This CFHT CassHawEC spectrograph was built in the period 1978–1983 under the responsibility of INSU technical division in Paris. Collimator and camera optics are a single convex-plane lens at f/8 and a 20-cm clear-aperture Schmidt plate, both passed twice through. The two telemeter beams are slightly decentered from the field of view and provide an auto-collimated access to the center of the detector.

Spherical aberration of the single lens spectrograph is corrected by a Schmidt plate that is virtually centered at the center of curvature of the lens spherical convex face. Although the telescope primary mirror pupil is naturally re-imaged near the echelle grating, a low powered lens before the telescope focal plane provides a rigorous pupil location (or stop) at the middle of this grating. The design provides high-resolution spectral imaging over a wide and square field of view.

The two off-axis mirror replicas are located slightly outside the circular Schmidt plate on opposite diametric directions. They directly reflect light at the detector through the



spectrograph single lens passed twice—without reaching the Schmidt plate and dispersers. The mirror replicas and spectrograph singlet lens act as a telemeter that allows checking the focusing set-up of the detector by fusion of two telemetric images (Figure 1).

**Figure 1.** Optical path scheme of the 20-cm pupil aperture CFHT-CassHawEc spectrograph including a field-lens (FL). The telemeter (T) uses two replica telemeter mirrors (TM) for the focusing set-up of a 2D detector (D). Each replica mirror TM compensates aberration of the convex-plane lens (L). Their shape provide an equivalent correction to that of the extended-size Schmidt plate (SP). Pair of pencil rays for telemeter in red color.

Lemaitre showed that active optics methods and elasticity theory [3–5] allow generating many freeform shapes for astronomical instrumentation. The present method was developed for making off-axis aberration corrective mirrors equivalent to that of a zonal Schmidt plate. It describes geometry of a quenched chromium stainless steel deformable matrix. The optical clear aperture is a sectorial contour. Elasticity theory led us to a prismatic radial thickness distribution that decreases when the off-axis direction increases.

Polished flat at rest, the matrix was used as submaster when bent for mirror replications via an epoxide resin on a glass substrate. We thus obtained plane-aspheric freeform replica mirrors that were used as a pair of correctors for a spectrograph telemeter. These corrector mirrors were mounted in opposite directions and slightly outside the Schmidt plate, thus allowing set-up focusing of the detector.

Those plane-aspheric replica mirrors compensate for third-order spherical aberration, *Sph-3*, which in a first approximation is locally equivalent to third-order astigmatism, *Astm-3*, but more accurately includes the coma mode, *Coma-3*.

# 3. Deformable Matrix Geometry and Elasticity Design

A quenched chromium stainless steel deformable matrix in Fe87Cr13 alloy from Ugima-4028 X30C13, Ugine, France (about similar to AISI-420 alloy), is selected. This alloy provides (*i*) a high deformability, (*ii*) an excellent linear stress–strain relationship and, (*iii*) an excellent ability for polishing.

Active area geometry of the deformable matrix is able to generate replicas that compensate for zonal spherical aberration *Sphe*-3 outside the 200-mm clear aperture diameter of a Schott UBK7 refractive Schmidt plate. The *rectangular* size of mirror replicas (TM in Figure 1) are  $20 \times 30 \text{ mm}^2$  in radial and tangential directions respectively.

The asphericity amount of the off-axis replicas is determined from the Schmidt plate and its central wavelength refractive index—as an equivalent correction transferred to the replica mirror shape. Of course, due to the replication process, the matrix and replica have opposite shapes.

The elasticity design of the deformable matrix (Figure 2) is made of three zones **A**, **B**, and **C**, in a single *holosterique* piece of a 24° angular sector,  $\theta = \pm 12^\circ$ , that defines a *bridge* as follows. **A**—an inner rigid unmovable zone. **B**—a deformable area of thickness

t(r) from  $r_1 = 105$  mm to  $r_2 = 125$  mm in radial directions, and that should be close to a rotational symmetry in the tangential direction. **C**—an outer rigid part able to rotate around a tangential axis and translate in the axial direction (Figure 2c).



**Figure 2.** Various views of the deformable matrix on its bending support after removing of replica plates: oblique, front, lateral and rear views of the matrix-support system, (**a**), (**b**), (**c**), and (**d**) respectively. In (**b**), dotted lines show the  $20 \times 30 \text{ mm}^2$  replica clear aperture area which is centered at 115 mm off-axis.

Round corners of radius 1 mm are designed at the junctions of zones **A-B** and **B-C**, thus avoiding stress concentrations.

Boundary conditions of the deformable zone **B** are:

- 1. Built-in link at the curved outer zone A and also for curved inner zone C,
- 2. Free-edge along the straight lines of the sector bridge.

The integration of elasticity equation, for determining the thickness t(r) of deformable zone **B** in radial direction, is derived from the wavefront curvature variation of the Schmidt plate correction. Zone **B** remains of constant thickness along the two concentric circles, and centered at the summit of angle 24° of the sector bridge, i.e., the center of the original full aperture Schmidt plate.

The Schmidt plate shape is classically represented by  $z = (N - 1)(A_{2SP} r^2 + A_{4SP} r^4)$ . In the third-order optics theory the radial curvature variation of a Schmidt plate that compensates spherical aberration can be defined only by a fourth power radial term. Similarly for zone **B** (Figure 2c), in cylindrical coordinates, the shape of the matrix to generate by flexure is of the form

$$z = (N-1)A_{4SP}r^4 = A_4r^4 \text{ and } r_1 \le r \le r_2, \tag{1}$$

where the first term represents the third-order term of the Schmidt Plate figure, and the last term is relative to the matrix figure to generate. The  $r_1$ ,  $r_2$ , radial limits define the annular area where the two telemeter mirrors are replicated from the active matrix.

Because the telemeter replica mirror-pair is just located outside the Schmidt plate, the optical design at f/8 is expanded at f/6.2 by just increasing the beam clear-aperture. One selects hereafter the He-Ne wavelength,  $\lambda = 632.8$ -nm, for optical testing. Considering only the 4th-power term of the even aspheric *refractive* UBK7 Schmidt plate, one has

 $A_{4-\text{SP}} = -5.012 \times 10^{-10} \text{ mm}^{-3}$ . An identical wavefront correction can be obtained for a *reflective* element. The mean refractive index is N = 1.515. Then the matrix correction, used as a mirror, is 1/(N-1) times smaller in deformation amplitude than the Schmidt plate passed twice through. Taking into account the fact that a segment mirror—replicated from the matrix—leads to an opposite shape, one selects coefficient  $A_4$  as

$$A_4 = (N-1)A_{4SP} = -2.582 \times 10^{-10} \text{mm}^{-3} \text{ and } r_0 = \frac{r_1 + r_2}{2} = 115 \text{ mm}$$
 (2)

for the matrix when bent and  $r_0$  for the segment mean off-axis distance respectively.

The matrix curvature function C(r), or second order derivative, is expressed in radial direction by

$$C(r) = \frac{d^2 z}{dr^2} \equiv \frac{1}{R(r)} = 12A_4 r^2,$$
(3)

where the curvatures are all concave.

The thin plate theory of small deformations defines classically the rigidity D(r) of a plate as [3,6]

$$D(r) = \frac{Et^{3}(r)}{12(1-\nu^{2})}$$
(4)

where E = 205 GPa is the Young modulus and  $\nu = 0.315$  the Poisson's ratio of the matrix in Fe87Cr13 alloy, and t(r) the thickness. Assuming in a first approximation that the matrix is bent into a rectangular surface (cf. T & WK [11], p. 5), the flexural moment in radial direction is express as:

$$M_r = D(r)\frac{d^2z}{dr^2} \propto t^3(r)r^2 \tag{5}$$

where the right term includes the substitution of Equations (3) and (4).

The equilibrium of the bridge (zone **B**) is achieved when the bending moment at the boundaries are equalized without applying any external load on the plate. Then  $M(r_1) = M(r_2)$  entails, since radial moments are constant along the bridge,

$$t_2^3 r_2^2 = t_1^3 r_1^2 = t_0^3 r_0^2 \tag{6}$$

which allows determination of  $t_2$  either from  $t_1$  or  $t_0$ , and where the thickness  $t_0$  holds for the radius  $r_{0.}$ 

A convenient calculation of the maximal radial stress  $\sigma_{r-Max}$  leads us to (cf. T & WK [11], p. 5)

$$\sigma_{rMax} = \frac{Et_0 C(r_0)}{2(1-\nu^2)}.$$
(7)

Setting  $t_0 = 4.70$  mm for  $r_0 = 115$  m, the bridge thickness t(r) decreases in radial direction since one obtains

$$t_1 \equiv t(r_1 = 105 \text{ m}) = 5.00 \text{ mm}, t_2 \equiv t(r_2 = 125 \text{ m}) = 4.45 \text{ mm}.$$
 (8)

This result leads us to a secure maximum stress,  $\sigma_r \cong \pm 27$  MPa, which is much lower than the stress at 0.2% elongation of  $\sigma_{0.2} = 650$  MPa as given by UGIMA Corp. for the 4028 material [12].

Although an off-axis zonal *Sph-3* correction may be mainly assimilated as an astigmatism correction *Astm-3*, one prefers—instead of a constant thickness plate—taking into account the radial thickness variation as derived from the above law,  $t^3r^2 = constant$ (cf. Equation (6)), which provides also coma correction *Coma-3*.

For practical reason due to machining of the bridge, the thickness of zone **B** is made as *varying linearly* in radial direction, i.e., a *conical shape* where the thickness is constant in the tangential direction.

## 4. Deformable Matrix-Modeling and Optical Testing

# 4.1. Matrix Aspheric Shape and Modeling

A preliminary modeling with Zemax code allows determining the optical patterns obtained at a surface area ( $\Delta Y = 20 \times \Delta X = 30$ )-mm<sup>2</sup> in size and off-centered of Y = 115-mm (see Figure 2b). Then the spectrograph design at f/8 is extended to f/6.2 for getting room to the telemeter mirrors that are diametrically opposite at the level of the Schmidt plate. The aspheric  $A_4$  coefficient is given by Equation (2). Image through focus shows the astigmatic pencil sections—before and after *Sph3* aberration correction—with the spectrograph lens passed twice (Figure 3a,b). Image at focus shows the quasi-astigmatism wavefront aberration, mainly *Astm3*, before correction of the telemeter mirror (Figure 3c).





#### 4.2. Modeling Optical Test with an Off-Axis Reflecting Image Transport

Setting now the origin of an *x*, *y*, *z* coordinate system at the center of the matrix replica area, the aspheric sags are

$$z_x = C_x h_x^2 / 2, z_y = C_y h_y^2 / 2 \text{ with } h_x = \Delta X / 2, h_y = \Delta Y / 2, \tag{9}$$

where  $h_x$  and  $h_y$  are semi-aperture sizes.

From the value of the matrix coefficient  $A_4$  in Equation (2) and the curvature expressed by Equation (3), the radial curvature is  $C_0 = 12A_4 r_0^2$ , where  $r_0 = 115$  mm at center of the segment. Assimilating the matrix shape locally as a *cylindrical shape*,  $C_x = 0$  and  $C_y = C_0$ , leads us to the sags

$$z_x = 0 \text{ and } z_y = 6 A_4 r_0^2 h_y^2.$$
 (10)

For a circular matrix area of  $\Delta Y = \Delta X = 30$  mm diameter the *cylindrical sag* in the *y*-direction is  $z_y = 4.61$ -µm PTV, which corresponds to 7.28 He-Ne fringes, i.e., an optical path difference of 14.56 He-Ne fringes with respect to flat reference.

We consider hereafter two options for optical testing of the matrix.

• OPTION 1–A null-test mounting: A finite distance optical design where a punctual off-axis source object illuminates a doublet lens and a *flat mirror* used over a 30-mm circular aperture area. The beams are passed twice through the achromatic lens of focal length F = 500 mm which are free from *Sph3* aberration (Figure 4a). The beam image shows astigmatism mode *Astm3*. Zemax optimization allows determining the principal beam off-axis deviation angle between the source object and its image that provides the same amount of *toric sag* (Figure 4b) than that of the previous *cylindrical sag* of the matrix when actively deformed. The deviation angle  $2\theta = 15^{\circ}$  corresponds to an object and image heights of 66 mm. The astigmatism length between sagittal and tangential foci is L = 20 mm.



**Figure 4.** Finite distance mounting with a flat mirror 30-mm circular clear aperture and an achromatic lens passed twice through. This mounting (**a**) provides an equivalent astigmatism sag amount (**b**) than that of the matrix.

This null-test mounting is performed by replacing the flat mirror by the bent matrix.

 OPTION 2–Twyman-Green Interferometric mounting: The reflected wave of the planeaspheric deformed matrix is compared to the reflected wave of a plane reference mirror in a two-arm interferometer. The result obtained from this option is presented hereafter.

#### 4.3. Matrix Active Optics Set-Up and Interferometric Result

After realization and flat polishing of the matrix when unstressed, the flexural elastic bending is achieved by screw actuators that generate a tangential rotation and an axial translation of zone **C**. The centering of replicas is at 115 mm off-axis radial distance. A gold coating allowed separation of mirror replicas.

Controlled rotation and translation of zone **C** about a rigid stand ( $84 \times 120$  mm) generate a *concave aspheric* shape in radial direction. The aspheric amount of local *Sph3* aberration of the matrix is set for a mirror correction as equivalent to the wavefront correction generated by the refractive Schmidt plate.

Two actuator screws, at zone C, generate set-up of the deformable aspheric surface. These are a pulling screw **Sc1** and a pushing screw **Sc2** near the edge (Figure 2d). The rectangular mirror replicas were  $20 \times 30$ -mm aperture, 6-mm thickness, on glass substrates by using epoxide polymer resin.

Optical testing of the matrix deformation is considered over a 20  $\times$  30-mm area. The image of this area is obtained via a CCD camera and a positive objective lens of the Twyman-Green interferometer. The monochromatic light source with an interferential filter at  $\lambda = 650$  nm, 4-nm band-pass, allows providing interferogram data reduction with Quick Fringes code (Figure 5).

## 4.4. Interpretation and Discussion of the Results

The set-up of the screw actuators, **Sc1** and **Sc2** (Figure 2d), is adjusted up to obtain satisfactory results from the theoretical request. From Table in Figure 5b, the Peak-to-Valley toroidal shape corresponds to 5.8 He-Ne fringes (633 nm) for 20 mm aperture in radial direction. Comparing astigmatism—showing a slightly *toric shape* in Figure 5a and a *saddle-like shape* in Figure 5c—provides results in close agreement together. For a 30-mm aperture in radial direction this would leads us to  $(30/20)^2$  times = 13.1 He-Ne fringes PTV compared to 14.2 and 14.5 fringes as displayed in Sections 4.1 and 4.2 respectively.



**Figure 5.** Synthetic fringes of the deformed matrix under test (**a**), aberration table analysis (**b**), and surface plot (**c**). The freeform matrix optical test is reduced with Quick Fringes at  $\lambda$  = 650 nm with 5.72-fringe astigmatism PTV, i.e., 5.8 He-Ne fringes over 20 × 30mm area.

The error is small, of the order one fringe i.e., 7% deviation. The *coma* term of 1.3 fringe in Table Figure 5b is mainly due to our matrix prismatic thickness design that should provide a complement aberration correction. From the table of Figure 5b, it can be seen that the zonal *spherical* aberration is negligible. One may notice from Figure 5a that the *anticlastic* effect of the flexure is found negligible over the tangential direction since it is smaller than a quarter of He-Ne fringe.

## 5. Conclusions

Present results from the matrix *toroidal shape* show that, for beams passed twice at the spectrograph, the wave-front error is close to one He-Ne wavelength. This provides satisfactory results for the telemeter-focusing device, which then is quasi-diffraction-limited.

The bridge of the matrix used for replications is with a *conical thickness*. Instead of a *constant thickness*, this allows including higher order corrections of the zonal Schmidt plate. This provides best modeling by generating zonal aberration corrections equivalent to astigmatism and coma corrections.

Active optics replication techniques from a deformable matrix can be applied to the construction of one or two *zonal Schmidt plate segments* for a pupil relay Schmidt-Offner imager. This unit magnification *ideal imager relay* was proposed by Rakich [1,2] for LGSAO and also proposed by Ciliegi et al. [13] for laser tomography adaptive optics (LTAO). For various distances of earth's atmospheric layers, the *volume spaces* of projected pupils are exempt from all five Seidel aberrations and from pupil aberrations.

Such zonal Schmidt plates, as replicated from an active matrix, may potentially provide an *ideal imager relay* solution. Extremely smooth surfaces contribute widely to perform high-angular resolution.

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Conflicts of Interest: The authors declare no conflict of interest.

#### Nomenclature

AO	Active Optics and/or Adaptive Optics
CassHawEC	Cassegrain Spectrograph of Hawaii Electronic Camera-CFHT
CCD	Charge Coupled Device
CFHT	Canada France Hawaii Telescope
EC	Electronic Camera
FireBall	Faint Intergalactic Redshifted objects for Balloon observations
LAMOST	Large Sky Area Multi-Object Fiber Spectroscopic Telescope
LGSAO	Laser Guide Star Adaptive Optics
LTAO	Laser Tomography Adaptive Optics
MESSIER	Telescope project dedicated in memory to astronomer Charles MESSIER
PtV or PTV	Peak to Valley
UBK7	Borosilicate-Crown in grade U, index ref. [7], by Schott Corp.

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